Channel Structures Based on Octahedral Frameworks: The Crystal Structure of $TITi_5Se_8$, TIV_5Se_8 , and $TICr_5Se_8$ and Its Relationships to $TICr_3S_5$, Hollandites, and Psilomelane*

K. KLEPP

Institut für Anorganische Chemie der Technischen Hochschule, Aachen, Prof. Pirlet-Str. 1, D-5100 Aachen, BRD

AND H. BOLLER[†]

Institut für Physikalische Chemie der Universität Wien, Währingerstr. 42, A-1090 Wien, Austria

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TITi₅Se₈, TIV₅Se₈, and TICr₅Se₈ are monoclinic, space group C2/m, Z = 2, TIV₅S₈ type with lattice parameters

a = 18.773(2), *b* = 3.5834(1), *c* = 9.1065(7)Å, β = 104.13(1)° (TITi₅Se₈) *a* = 18.354(1), *b* = 3.4656(1), *c* = 8.9036(3)Å, β = 104.03(1)° (TIV₅Se₈) *a* = 18.699(1), *b* = 3.5942(1), *c* = 8.9418(9)Å, β = 104.70(1)° (TICr₅Se₈).

A unified scheme is developed for the TIV_5S_8 , $TICr_3S_5$, hollandite, and psilomelane structures on the basis of ideal close packing.

Introduction

In the course of a study on ternary chalcogenides of thallium and the early transition metals we prepared a series of isotypic compounds TlT_5Se_8 (T = Ti, V, Cr) crystallizing with the TlV_5S_8 structure type (1). There is an apparent similarity of this typical tunnel structure to the $TlCr_3S_5$ structure type (2) on the one side and to hollandite and psilomelane on the other side. In view of the current interest in compounds with tunnel structures as model substances for one-dimensional ionic conductivity, it was promising to investigate the structural relationships between these compounds in more detail.

Experimental

The title compounds were prepared from TISe, Se, and the corresponding transition metal. Stoichiometric amounts of the powdered components were intimately mixed and sealed into evacuated silica tubes. The samples were gradually heated to 1350 K, kept at this temperature for several days, and finally allowed to cool to ambient temperature in the course of three weeks. Welldeveloped single crystals of appropriate size for X-ray investigations could be iso-

^{*} Dedicated to Professor M. J. Sienko on the occasion of his 60th birthday.

[†] Author to whom correspondence should be addressed.

lated from the crushed samples. The compounds crystallize in the form of elongated rectangular platelets and exhibit metallic luster.

Preliminary crystallographic investigations performed with rotating crystal and Weissenberg techniques showed Laue symmetry 2/m, the unique crystallographic axis being coincident with the long crystal axis. Systematic extinctions were observed for *hkl*: h + k = 2n indicating C2/m, C2, or Cm as possible space groups. The dominating habitus planes are parallel to (001); preferred cleavage occurs along [010]. Rotating crystal photographs of crystals turned around the axis perpendicularly to the habitus plane showed a pronounced rhombohedral subcell. The similarity of the lattice dimensions and of the relative intensities suggested that the three compounds were members of an isotypic series.

The lattice constants given in the abstract were obtained by least squares refinement of the 2θ values of 32 reflections measured on a computer controlled four circle diffractometer (Philips PW 1100, graphite monochromated Mo $K\alpha$ radiation).

Integrated intensities were collected with continuous θ -2 θ scans up to a sin θ/λ limit of 0.64. The usual background, Lorentz, and polarization corrections were applied. Absorption effects were accounted for by a spherical absorption correction. Equivalent reflections were averaged yielding unique sets of 684 (TITi₅Se₈), 647 (TIV₅Se₈), and 409 (TICr₅Se₈) observed intensities with $I \ge 3 \sigma(I)$.

Structure Refinement

Composition, symmetry, and lattice dimensions indicated isotypy with $TIV_5S_8(1)$. Least squares refinements were hence started in space group C2 with the atomic positions of TIV_5S_8 . The y parameter of TI was arbitrarily fixed at 0.0. A critical inspection of the results showed that during the refinements the free y parameters had been shifted close to the special values 0.0 and 0.5, which was taken as an indication that the correct space group was C2/m. This was also suggested by the statistics of the normalized structure factors and by the fact that the isostructural compounds ACr_5S_8 ($A = K, Rb, Cs, Ba_{0.5}$) have been refined in the centrosymmetric space group (3, 4). Refinement in C2/m yielded only insignificantly higher R values (TlTi₅Se₈: R = $0.040 \text{ vs} 0.040, \text{TlV}_5\text{Se}_8$: R = 0.066 vs 0.064, $TlCr_5Se_8$: R = 0.059 vs 0.058. All calculations were performed with programs of the X-Ray system (5). Scattering factors for neutral atoms were taken from Cromer and Mann (6), corrections for anomalous dispersion from the International Tables for X-Ray Crystallography (7). The final positional and thermal parameters are given in Table I. The significant interatomic distances are compiled in Table II. Lists of the $|F_0|$ values can be obtained from the authors on request.

Discussion

The compounds $TlTi_5Se_8$, TlV_5Se_8 and $TlCr_5Se_8$ are isotypic and crystallize with the TlV_5S_8 structure type (1). The crystal structure is characterized by a three-dimensional framework of TX_6 -octahedra (T =transition metal, X = chalcogen) sharing edges and faces to form channels parallel to [010] which accommodate the thallium atoms. The transition metal atoms are on three different crystallographic sites. In consideration of the type of connection their coordination octahedra are not equivalent. The octahedra centered by T(1) (in the special position 4d) are connected to those centered by T(3) by common edges. The octahedra centered by T(2) and by T(3)have one face in common.

The present series TIT_5Se_8 allows one to study the influence of the transition metal on the crystal structure. The unit cell vol-

KLEPP AND BOLLER

Atom	Position	x	у	z	$U_{11}{}^a$	U_{22}	U_{33}	U_{12}	U_{13}	U_{23}
Tl	2 <i>a</i>	0	0	0	5.67(5)	3.11(5)	3.55(4)		1.28(3)	·
Ti 1	2 <i>d</i>	0	0.5	0.5	0.82(8)	0.94(9)	0.40(7)	_	0.02(6)	_
Ti 2	4 <i>i</i>	0.7919(1)	0	0.1510(1)	0.82(6)	0.81(7)	0.40(6)	—	0.01(4)	
Ti 3	4 <i>i</i>	0.1540(1)	0	0.4939(1)	1.01(6)	0.93(7)	0.57(6)	—	0.08(4)	
Se 1	4 <i>i</i>	0.6606(0)	0	0.0007(1)	0.94(4)	0.91(5)	0.55(4)	—	0.07(3)	
Se 2	4 <i>i</i>	0.2584(0)	0	0.3382(1)	0.97(4)	0.72(4)	0.46(4)	—	0.23(2)	
Se 3	4 <i>i</i>	0.5860(0)	0	0.3162(1)	1.00(4)	1.01(5)	0.57(4)	_	0.12(3)	
Se 4	4 <i>i</i>	0.9268(0)	0	0.3233(1)	0.76(4)	0.90(5)	0.45(4)	_	0.02(3)	_
				R = 0.0	$140 (R_w = 0.0)$)49)				
Tl	2 <i>a</i>	0	0	0	2.74(5)	2.75(6)	2.69(6)	—	0.67(4)	
V 1	2 <i>d</i>	0	0.5	0.5	0.49(11)	2.44(14)	0.82(11)	—	0.09(8)	_
V 2	4 <i>i</i>	0.7900(1)	0	0.1479(2)	0.26(8)	1.80(10)	1.16(9)	—	0.28(6)	_
V 3	4 <i>i</i>	0.1490(1)	0	0.4955(2)	0.41(8)	1.53(9)	1.01(8)	_	0.18(6)	_
Se 1	4 <i>i</i>	0.6595(1)	0	0.0021(1)	0.36(5)	1.27(7)	1.16(6)		0.18(4)	
Se 2	4 <i>i</i>	0.2583(1)	0	0.3418(1)	0.39(6)	1.00(6)	1.02(6)		0.271(4)	_
Se 3	4 <i>i</i>	0.5849(1)	0	0.3151(1)	0.58(6)	1.20(6)	1.01(6)		0.25(4)	_
Se 4	4 <i>i</i>	0.9278(1)	0	0.3178(1)	0.36(6)	1.14(6)	1.17(6)	_	0.24(4)	—
				R = 0.0	$66 (R_w = 0.0)$)6 4)				
Tl	2 <i>a</i>	0	0	0	13.0(4)	2.5(2)	3.7(2)	_	1.2(2)	—
Cr 1	2 <i>d</i>	0	0.5	0.5	0.8(3)	0.3(3)	0.9(3)		0.2(3)	—
Cr 2	4 <i>i</i>	0.7954(3)	0	0.1664(6)	0.9(2)	0.5(2)	0.9(2)	_	0.1(2)	_
Cr 3	4 <i>i</i>	0.1571(3)	0	0.4819(6)	1.0(2)	0.6(3)	0.7(2)		0.3(2)	_
Se 1	4 <i>i</i>	0.6681(2)	0	0.9930(4)	1.1(2)	0.3(1)	0.8(1)		0.3(1)	
Se 2	4 <i>i</i>	0.2604(2)	0	0.3425(4)	1.1(2)	0.1(1)	1.0(2)		0.4(1)	
Se 3	4 <i>i</i>	0.5850(2)	0	0.3211(4)	1.2(2)	0.3(2)	1.0(1)		0.2(1)	_
Se 4	4 i	0.9262(2)	0	0.3387(4)	0.7(1)	0.5(2)	0.9(1)		0.1(1)	

TABLE I

Positional and Thermal Parameters of TITi3Se8, TIV3Se8, and TIC13Se8 (Space group C2/m)

^{*a*} The U_{ij} are multiplied by 100.

TITi ₅ Se ₈		TIV ₅ Se ₈		TlCr ₅ Se ₈		
Tl -Sel	3.506(1) (4×)	Tl-Se1	3.398(1) (4×)	Tl-Se1	3.635(3) (4×)	
-Se3	3.441(9) (4×)	-Se3	3.344(4) (4×)	-Se3	3.418(3) (4×)	
-Se4	3.540(8) (2×)	-Se4	3.403(4) (2×)	-Se4	3.633(4) (2×)	
Ti1–Se3	2.594(6) (2×)	V1–Se3	2.526(4) (2×)	Cr1-Se3	2.525(4) (2×)	
-Se4	2.571(6) (4×)	-Se4	2.519(3) (4×)	-Se4	2.491(2) (4×)	
Ti2-Se1	2.511(9), 2.552(3) (2×)	V2-Se1	2.433(5), 2.499(2) (2×)	Cr2-Se1	2.490(6), 2.494(5) (2×)	
-Se2	2.653(3) (2×)	-Se2	2.610(2) (2×)	-Se2	2.581(5) (2×)	
-Se4	2.633(10)	-Se4	2.613(5)	-Se4	2.537(6)	
Ti3-Se2	2.686(7), 2.651(6) (2×)	V3–Se2	2.689(4), 2.608(3) (2×)	Cr3-Se2	2.550(7), 2.616(4) (2×)	
-Se3	2.539(5) (2×)	–Se3	2.460(3) (2×)	-Se3	2.476(4) (2×)	
-Se4	2.510(7)	-Se4	2.426(4)	-Se4	2.504(7)	
Til-Ti3	$3.412(1)(4\times)$	V1–V3	3.246(2) (4×)	Cr1–Cr3	3.483(5) (4×)	
Ti2–Ti2	3.337(9) (2×)	V2V2	3.198(4) (2×)	Cr2–Cr2	3.523(5) (2×)	
-Ti3	3.144(7)	-V3	3.100(4)	-Cr3	3.042(7)	

TABLE II Interatomic Distances (in Å)

umes (593.6, 549.3, and 581.3 Å³ for TITi₅Se₈, TIV₅Se₈, and TlCr₅Se₈, respectively) do not vary smoothly as might be expected from the atomic radii of Ti, V, and Cr. The unit cell volume of TIV₅Se₈ is by ~6% smaller than that of $TlCr_5Se_8$. The same trend is also observed with binary selenides, e.g., the phases with compositions near TSe (8-10) (NiAs type) and composition $T_3Se_4(11)$ (T = Ti, V, Cr). By comparison of the interatomic distances in the TlT_5Se_8 phases (Table II) one is led to tentatively attribute the smaller unit cell volume of TIV_5Se_8 to increased T-T interactions: The mean T-Se distance decreases continuously from TlTi₅Se₈ to TlCr₅Se₈. The smallest value for the average T-T distance is, however, observed in the vanadium compound. While in TlCr₅Se₈ the distance Cr(2)–Cr(3) corresponding to the face sharing octahedra is clearly shorter than the Cr-Cr distances corresponding to edge sharing, the difference is less pronounced in TIV_5Se_8 . Here the atoms V(2) and V(3) are displaced from the centers of the octahedra giving rise to the formation of shorter distances $(d_{V(1)-V(3)} = 3.246 \text{ Å}, d_{V(2)-V(2)} =$ 3.198 Å). TITi₅Se₈ takes an intermediate position.

The average Se–Se distance is 3.63 Å in TITi₅Se₈, 3.54 Å in TIV₅Se₈, and 3.58 Å in TICr₅Se₈. The size of the channels varies considerably, as can be seen from the Tl–Se distances. The average Tl–Se distance in TIV₅Se₈ (3.377 Å) is close to the sum of the ionic radii for Tl⁺ and Se²⁻ (1.40 + 1.98 Å). In TITi₅Se₈ and TICr₅Se₈ the average Tl–Se distance is distinctly larger. This is reflected by an elevated temperature factor U_{11} of Tl in both compounds.

A General Construction Scheme for the TIV_5S_8 , the $TICr_3S_5$, the Hollandite, and the Psilomelane Type of Structure

The TlV₅S₈ structure type is closely related to the TlCr₃S₅ type (Figs. 1a,b). Both

structures are characterized by three dimensional frameworks of TX_6 octahedra with channels accommodating one (TIV₅S₈) or two (TlCr₃S₅) rows of thallium atoms. These structural relationships correspond to those of the hollandite family (12) and psilomelane (13) (Figs. 1c,d).

The four structure types can be derived from a mixed close packed structure formed by the anions X, together with the large cations M. The small cations T (mainly transition metal ions) occupy the octahedral interstices formed by the anions only. The stacking of the close packed layers is hhc. The c layers are mixed, the h layers consist of anions only.

Two kinds of ordered layers can be distinguished: one with stoichiometry MX_2 in the TlV₅S₈ type and in the hollandites, the other one with stoichiometry MX in the TlCr₃S₅ type and in psilomelane (Fig. 2).

Based on ideal close packing the four structure types can be consistently described with monoclonic unit cells showing the following common features.

- (a) The channels are parallel to the direction of the unique axis b, the length of this axis corresponding to the elementary translation $(a_{\rm H})$ within the close packed layers disregarding chemical order (Fig. 2).
- (b) The close packed layers are parallel to one of the basal planes (001) or (100). For the sake of convenience this plane will be defined as (001) in this discussion. For this purpose TlCr₃S₅ and psilomelane are set up in the nonstandard space group A2/m.
- (c) The elementary stacking vector between two layers is parallel to the (010) plane with components **p** and **s** parallel and perpendicular to the [100] direction. The length of **p** is given by $p = a_{\rm H}\sqrt{3}/3$, the length of **s** by $s = a_{\rm H}\sqrt{2}/3$.

The crystal structures and their unit cells can be described in terms of $a_{\rm H}(=b)$ and





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KLEPP AND BOLLER

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three integers:

- *l*: length of a in units of p ($a = l \times p$),
- *m*: distance between two equivalent ordered layers in units of *s* (number of layers),
- n: lateral displacement between two equivalent ordered layers in units of p.

By the latter two definitions the stacking vector t between two equivalent ordered layers is t = ms + np. The following relationships can easily be derived:

$$tg(\beta - 90^{\circ}) = \frac{np}{ms} = \frac{1}{\sqrt{2}} \frac{n}{m}$$

or $tg\beta = -\frac{1}{\sqrt{2}} \frac{n}{m}$
 $\frac{a}{b} = \frac{l}{\sqrt{3}}$
 $\frac{c}{a} = \sqrt{2} \frac{m}{l \sin \beta}.$

An orthogonal unit cell can be obtained consisting of $l \times m$ layers with $a_{ortho} = a$, $b_{ortho} = b$, $c_{ortho} = l \times m \times s$.

The values of l, m, and n are not arbitrary: l is determined by the ordering in the mixed layer (e.g., 9 and 6 for MX_2 and MX layers, respectively). m must be a multiple of 3 because of the *hhc* stacking sequence. n can adopt values given by

$$n=m/3+3n'.$$

For m = 3, n' can be an integer $0 \le n' < l/3$. In the case of m = 6 neighboring ordered layers are not equivalent, having a stacking vector with a nonintegral component perpendicular to s, given by $(1 \pm 3/2)\mathbf{p} + \mathbf{b}/2$. Therefore the stacking vector to the next equivalent layer is $\mathbf{t} = 6\mathbf{s} + (2 \pm 3)\mathbf{p}$ (i.e., n' $= \pm 1$).

As seen from Table III the subseries with l = 9 (*MX*₂ layers) contains one more hypothetical structure besides the TlV₅S₈ type and the hollandite type. The subseries with

TABLE III Possible Channel Structures Based on Close Packing Defined in Terms of *l. m.* and *n*

ı	m	n Structure type
9	3	1 TIV ₅ S ₈
6	3	$\begin{cases} 4 & \text{Hollandite} \\ 7 \\ 1 \\ 4 \end{cases}$ Hypothetical structures
6	6	-1^a Psilomelane 5 TlCr ₃ S ₅

^a A negative value of *n* corresponds to a unit cell with an acute angle β . Choosing |n|, an equivalent setting with a unit cell having $\beta' = 180 - \beta$ is obtained.

l = 6 (*MX* layers) and m = 6 has only two members, realized by the TlCr₃S₅ type and by psilomelane. It should be noted that in these two structures the stacking of the equivalent mixed layers (i.e., every second mixed layer) is the same (because of $n \equiv -1$ mod $6 \equiv 5 \mod 6$). There are two hypothetical structures with *MX* layers and m = 3.

Within one subseries (i.e., for a given land m) the different lateral displacement of the mixed layers, as characterized by n, leads to a different arrangement of the channels. In the oxide phases the channels form an almost orthogonal array (Figs. 1c,d). As a consequence the oxygen octahedra at the corners of the channels share two opposite faces with neighboring octahedra. These octahedra are not occupied by T atoms. In the chalcogenide phases the arrangement of the channels requires only



FIG. 2. The two anion-cation mixed layers of composition MX_2 and MX. The pseudo-hexagonal cell (a_H) and the component 3p of the stacking vector between equivalent layers are also shown.

one face to be shared, and all chalcogen octahedra are occupied. Therefore the stoichiometries of the $[T_mX_n]$ frameworks in TIV_5S_8 and $TICr_3S_5$ are different from those in hollandite $[T_4O_8]$ and psilomelane $[T_5O_{10}]$, respectively.

The unit cell dimensions of the known compounds crystallizing in the TlV₅S₈ and TlCr₃S₅ types of structure are listed in Table IV. The very good agreement between β , a/b, and c/a calculated for the ideal model and the values of the real structures of the chalcogenide phases is remarkable in view of the apparent deformations observed on the local scale. Greater deviations from the ideal model are present in the hollandites and psilomelane, for which two representatives, monoclinic Ba_{0.7}Sn_{2.6}Cr_{1.4} O₈ (14) and monoclinic (Ba,H₂O)₂Mn₅O₁₀ (13) are included in Table IV. In the hollandite phases the deviations from the sphere packing model tend to enhance the pseudo-tetragonal symmetry of the structure. Actually some hollandites are tetragonal (12, 15). The relations between the monoclinic cell as derived from the sphere packing model, and the (pseudo) tetragonal cell can be seen from Fig. 1c and Ref. (14).

The question of ionic mobility in cation deficient hollandites is controversial (16). The title compounds do not indicate nonstoichiometry with respect to thallium. The crystals, however, have been picked up from samples prepared at stoichiometric compositions. In the case of the isotypic sulfide TIV₅S₈, Schöllhorn *et al.* (17) report on the electrochemical topotactic extraction of thallium and its electrochemical exchange against lithium. These authors postulate mobility of the cations within the channels of the $[V_5S_8]$ framework at room

	a(Å)	b(Å)	c(Å)	β(°)	a/b	c/a		
	17.465	3.301	8.519	103.94	5.29	0.488		
TITi _s Se ₈	18.773	3.583	9.1065	104.13	5.24	0.485		
TIV Se.	18.354	3.4656	8.9036	104.03	5.30	0.485		
TICr ₅ Se ₈	18.699	3.5942	8.9418	104.70	5.20	0.478		
KCr _s S ₈	17.798	3.447	8.598	105.00	5.16	0.483		
RbCr _s S ₈	17.835	3.452	8.654	104.74	5.17	0.485		
CsCr ₅ S ₈	17.915	3.464	8.732	104.62	5.17	0.487		
Ban CrsSe	17.771	3.425	8.566	104.68	5.19	0.482		
Ideal				103.26	5.10	0.484		
TICr ₃ S ₅ ^a	11.98	3.454	19.29	122.1	3.47	1.61		
TICr ₃ Se ₄	12.40	3.59	20.08	121.3	3.45	1.62		
Ideal				120.51	3.46	1.64		
$Ba_{0.7}Sn_{2.6}Cr_{1.4}O_8$ (holtandite	14.728	3.108	10.012	134.37	4.47	0.680		
Ideal				133.31 ^b	5.20	0.648		
$(Ba,H_2O)_2Mn_5O_{10}^a$ (psilomelane)	9.56	2.88	13.85	92.50	3.32	1.45		
Ideal				96.72	3.46	1.42		

TABLE IV

UNIT CELL PARAMETERS OF COMPOUNDS WITH THE TIV₃S₈ and the TIC₁₅S₃ Type of Structure Including One Hollandite Phase and Psilomelane

^{*a*} Unit cell set up in A2/m.

^b $\beta = 93^{\circ}$ for the usual pseudotetragonal cell set up in space group I2/m.

temperature. In view of the higher polarizability of the anions and of the metallic character of the framework, nonstoichiometric transition metal sulfides and selenides with channel structures are probably more realistic model substances for one-dimensional ionic conductivity than oxide phases. This should be especially true for the vanadium and titanium compounds.

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References

- 1. L. FOURNÈS, M. VLASSE, AND M. SAUX, Mater. Res. Bull. 12, 1 (1977).
- 2. CHR. PLATTE AND H. SABROWSKY, Naturwissenschaften 60, 474 (1973).
- 3. J. HUSTER, Z. Anorg. Allg. Chem. 447, 89 (1978).
- 4. J. HUSTER, Z. Kristallogr. 149, 146 (1979).

- 5. "X-Ray System," Tech. Rep. TR-446 (J. M. Stewart, Ed.), Computer Science Center, University of Maryland, College Park, Md. (1976).
- 6. D. T. CROMER AND J. B. MANN, Acta Crystallogr. A Sect. 24, 321 (1968).
- 7. International Tables for X-Ray Crystallography, Vol. IV, Kynoch Press, Birmingham, England (1974).
- 8. F. GRØNVOLT AND F. J. LANGMYHR, Acta Chem. Scand. 15, 1949 (1961).
- E. Røst and L. GJERSTEN, Z. Anorg. Allg. Chem. 328, 299 (1964).
- 10. F. H. WEHMEIER, E. T. KEVE, AND S. C. ABRA-HAMS, *Inorg. Chem.* 9, 2125 (1970).
- 11. M. CHEVRETON AND F. BERTAUT, C.R. Acad. Sci. Paris 255, 1275 (1962).
- A. BYSTRÖM AND A. M. BYSTRÖM, Acta Crystallogr. 3, 146 (1950).
- 13. A. D. WADSLEY, Acta Crystallogr. 6, 433 (1953).
- 14. M. C. CADÉE AND G. C. VERSCHOOR, Acta Crystallogr. Sect. B 34, 3554 (1978).
- 15. W. SINCLAIR, G. M. MCLAUGHLIN, AND A. E. RINGWOOD, Acta Crystallogr. Sect. B 36, 2913 (1980).
- L. A. BURSILL AND G. GRZINIZ, Acta Crystallogr. Sect. B 36, 2902 (1980).
- R. SCHÖLLHORN, W. SCHRAMM, AND D. FENSKE, Angew. Chem. 92, 477 (1980).